

integrate $\int 2x \cos x dx$

make $u = 2x$ and $\frac{dv}{dx} = \cos x$
 $dv = \cos x dx$

then $\frac{du}{dx} = 2$ and $v = \sin x$
 $du = 2 dx$

using the formula

$$\int u dv = uv - \int v du$$

$$\begin{aligned}\int 2x \cos x dx &= 2x \cdot \sin x - \int \sin x \cdot 2 dx \\ &= 2x \sin x - 2(-\cos x) + C \\ &= 2x \sin x + 2 \cos x + C\end{aligned}$$
